

## **MATHEMATICS PAPER 1 MEMORANDUM**

1.1.1 
$$2x^2 + 7x = 30$$
  
 $2x^2 + 7x - 30 = 0 \checkmark$   
 $(2x - 5)(x + 6) = 0 \checkmark$   
 $\therefore x = \frac{5}{2} \text{ or } x = -6 \checkmark \checkmark$ 
(4)  
1.1.2  $2x(x - 2) - 5 = 0$   
 $2x^2 - 4x - 5 = 0 \checkmark$   
 $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$   
 $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2x^2} \checkmark$   
 $x = \frac{4 \pm \sqrt{(-4)^2 - 4 \times (2)(-5)}}{2 \times 2} \checkmark$   
 $\therefore x = \frac{4 \pm \sqrt{56}}{4} \text{ or } x = \frac{4 - \sqrt{56}}{4} \checkmark \checkmark$   
Or  $x = 2,87 \text{ or } x = -0,87$ 
(4)  
1.1.3  $4x^2 + 7x - 2 < 0$   
 $(4x - 1)(x + 2) < 0 \checkmark \checkmark$   
 $+ \frac{-2}{4} \checkmark \frac{1}{4}$   
 $-2 < x < \frac{1}{4} \checkmark \checkmark$ 
(4)

1.2.1 
$$2x + 6 - y = 0$$
  
 $2x + 6 = y$   
 $y + 3x^2 = 8x + 3$   
 $y = -3x^2 + 8x + 3 \checkmark$  (5)

$$\therefore 2x + 6 = -3x^2 + 8x + 3 \checkmark$$

$$3x^2 - 6x + 3 = 0$$

$$x^2 - 2x + 1 = 0$$

$$(x - 1)^2 = 0 \checkmark$$

$$\therefore x = 1 \checkmark$$

$$\therefore y = 2x + 6 = 8 \checkmark$$
1.2.2

(1; 8) is the point of contact between the straight line y = 2x + 6 and the parabola  $y = -3x^2 + 8x + 3$ . There is one point of contact.  $\Rightarrow$  line is a tangent to the curve.

$$\Rightarrow \text{ line is a tangent to the curve. } \checkmark \qquad (3)$$
2.1
$$P = \frac{x \left[1 - (1+i)^{-n}\right]}{i} \checkmark$$

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(1)

(4)

(6)

(2)

(4)

(3)

$$800000 = \frac{7500}{9} \frac{1 - \left(1 + \frac{100}{12}\right)^{-n}}{\frac{100}{12}} \checkmark \checkmark$$

$$800000 = \frac{7500}{1 - \left(1 + \frac{3}{400}\right)^{-n}} \frac{1}{3}$$

$$800000 = \frac{7500}{1 - \left(1 + \frac{3}{400}\right)^{-n}} \frac{1}{3}$$

$$800000 = \frac{7500}{400} \frac{1 - \left(\frac{403}{400}\right)^{-n}}{\frac{3}{400}} \frac{1}{3}$$

$$800000 = \frac{3}{400} - 7500 - 1 - \left(\frac{403}{400}\right)^{-n} \frac{1}{3}$$

$$\frac{30}{25} = 1 - \left(\frac{403}{400}\right)^{-n} \checkmark \qquad (3)$$

$$\frac{30}{25} = 1 - \left(\frac{403}{400}\right)^{-n} \checkmark \qquad (5)$$

$$\frac{30}{25} = 1 - \left(\frac{403}{400}\right)^{-n} \checkmark \qquad (7)$$

$$\frac{30}{25} = 1 - \left(\frac{403}{100}\right)^{-n} \checkmark \qquad (7)$$

$$\frac{30}{21} = \frac{1}{100} \frac{1}{100} \frac{1}{100} \checkmark \qquad (7)$$

$$\frac{30}{100} = \frac{1}{100} \frac{1}{10} \frac{$$

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$$\begin{aligned} s_{n} &= \frac{2 \left[ 1 - \left( \frac{3}{4} \right)^{n} \right]}{1 - \frac{3}{4}} \\ &= 75,49 \\ &\therefore \text{ Depth is } 75,49 \\ &= \frac{-20}{1 - \frac{3}{4}} \\ &= \frac{20}{1 - \frac{3}{4}} \\ &$$

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$$A(x) = -\frac{3}{2}x^{2} + 24x \checkmark$$
  

$$\therefore \text{ let } 0 = -\frac{3}{2}x^{2} + 24x \checkmark$$
  

$$0 = x^{2} - 16x \checkmark$$
  

$$0 = x(x - 16)$$
  

$$x = 0 \text{ or } x = 16$$

∴ Maximum area will be covered after 16 months.  $\checkmark$ 

6.3.2 
$$A'(x) = -\frac{3}{2}x^2 + 24x$$
  
 $A'(1) = -\frac{3}{2}(1)^2 + 24(1) \checkmark$   
 $= 22\frac{1}{2}\checkmark$ 

$$\therefore$$
 The rate of growth was  $22\frac{1}{2}$  m<sup>2</sup>/ month  
one month after the study had begun.

7.1 one month after the study had begun. (2)  

$$f(x) = x^3 - 4x^2 - 3x + 18$$
  
 $f(3) = 27 - (4 \times 9) - (3 \times 3) + 18 = 0 \checkmark$  (1)

3 
$$f'(x) = 3x^2 - 8x - 3 = 0$$
 for turning points  
∴  $(3x + 1)(x - 3) = 0$   
 $x = -\frac{1}{3}$  and  $x = 3 \checkmark \checkmark$   
∴  $f(x) = (-\frac{1}{3})^3 - 4(-\frac{1}{3})^2 - 3(-\frac{1}{3}) + 18$   
 $= \frac{500}{27}$  (= 18,52)  $\checkmark$   
 $f(3) = 0$ 

$$\therefore$$
 Turning points at  $\left(-\frac{1}{3}; \frac{500}{27}\right)$  and  $(3; 0)$ .

7.4 
$$(5)$$
  
7.4 
$$(7.33,18.52)$$
  
(5)  
7.5 
$$f''(x) = 6x - 8 = 0 \checkmark$$
  
for point of inflection. (4)

$$\therefore x = \frac{8}{6} = \frac{4}{3} \checkmark$$
8.1  $V = \text{Area of base} \times \text{Height}$ 
2.5 =  $x^2 h \checkmark$ 
(2)

$$\frac{2.5}{x^2} = h \checkmark$$
(2)

8.2 Area = 
$$2(x^2 + 4xh) \checkmark$$
  
=  $2x^2 + 8x \times \frac{2.5}{x^2} \checkmark$  (3)

$$= 2x^{2} + \frac{20}{x}$$
  
8.3  $A = 2x^{2} + 20x^{-1}$   
 $\frac{dA}{dx} = 4x - 20x^{-2}$   
 $4x - \frac{20}{x^{2}} = 0$  (for minimum)  $\checkmark$   
 $\therefore 4x^{3} - 20 = 0$   
 $x^{3} = 5$   
 $x = \sqrt[3]{5} = 1,71$   $\checkmark$   
(5)  
9.1  $x = \text{no. of guitars of type A}$   
 $y = \text{no. of guitars of type B}$   
 $x + y \le 20$   
 $1500x + 3000y \le 45000$   $\checkmark$   
 $x \ge 6$   $\checkmark$   
9.2  
9.3  $P = 400x + 1000y$   $\checkmark$   
 $\frac{400}{1000} x + \frac{P}{1000} = y$   
 $\frac{2}{5}x + \frac{P}{1000} = y$   
 $\therefore$  Use search line of slope  $-\frac{2}{5}$  ... see  
sketch  $\checkmark$   
 $\therefore$  Maximum profit for  
 $x = 6$  and  $y = 12$  at point A.  $\checkmark$   
 $y = 500x + 1000y$   
 $\frac{500}{1000}x + \frac{P}{1000} = y$   
 $\therefore$  Use search line of slope  $-\frac{2}{5}$  ... see  
sketch  $\checkmark$   
 $\therefore$  Maximum profit for  
 $x = 6$  and  $y = 12$  at point A.  $\checkmark$   
 $y = 500x + 1000y$   
 $\frac{500}{1000}x + \frac{P}{1000} = y$   
 $\therefore$  Use search line of slope  $-\frac{2}{5}$  ... see  
sketch  $\checkmark$   
 $\therefore$  Maximum profit for  
 $x = 6$  and  $y = 12$  at point A.  $\checkmark$   
 $y = 500x + 1000y$   
 $\frac{500}{1000}x + \frac{P}{1000} = y$   
 $\frac{1}{2}x + \frac{P}{1000} = y$   
This line is parallel to one of the borders  
of the feasible region. Therefore  
maximum profit occurs at any whole-  
number point on this line.  $\checkmark$   
 $i.e. A(6; 12)$   
 $B(8; 11)$   
 $(3)$ 

(3)

C(10; 10) •