GRADE 12
DATE: August 2010

NAME: $\qquad$ TEACHER: $\qquad$

| QUESTION | MARKS | LO1 | LO2 |
| :---: | :---: | :---: | :---: |
| 1. | 12 |  |  |
| 2. | 11 |  |  |
| 3. | 14 |  |  |
| 4. | 13 |  |  |
| 5. | 23 |  |  |
| 6. | 19 |  |  |
| 7. | 14 |  |  |
| 8. | 10 |  |  |
| 9. | 23 |  |  |
| 10. | 11 |  |  |
|  |  |  |  |
| TOTAL | 150 |  |  |

Given: $f(x)=\frac{5}{x-3}-1$
a) What kind of graph does $f$ represent?
b) Write down the equations of the asymptotes of $f$. $\qquad$
c) Determine the intercepts with the axes. $\qquad$
$\qquad$
$\qquad$
$\qquad$
d) Sketch the graph of $f$, clearly showing all relevant features of this graph.

e) Give the new equations after the following transformations:

1) $\quad f(x)$ reflected about the $y$-axis $\qquad$
$\qquad$
$\qquad$
2) $f(x)$ translated 3 units to the right and 2 units up $\qquad$
$\qquad$
$\qquad$

Let $\boldsymbol{x}$ be the number of articles of model A and $\boldsymbol{y}$ be the number of articles of model B which can be manufactured daily by a factory, subject to the following constraints:

$$
\begin{aligned}
& x \geq 4 \\
& y \geq 6
\end{aligned}
$$

$$
\begin{gathered}
x+y \geq 12 \\
5 x+4 y \leq 80 \\
2 y+x \leq 28
\end{gathered}
$$

a) Represent all the constraints on the graph paper provided.

Clearly indicate the feasible region.

b) If it costs R300 to make each article of model A and R200 to make each article of model B, write down an equation to represent the total cost, $T$, to manufacture $x$ articles of model $A$ and y articles of model B . $\qquad$
$\qquad$
$\qquad$
$\qquad$ (2)
c) Draw on the graph a straight line that you would use to minimize the total production cost. $\qquad$
$\qquad$
$\qquad$
$\qquad$
d) Give the number of articles of each model that should be manufactured to ensure a minimum cost, and determine the minimum cost. $\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
e) If the manufacturing cost is adjusted and it now costs the same to manufacture models A and $B$, but it is not desirable to make more of model $A$ than of model $B$, determine how many of each should be manufactured to ensure minimum expenditure. $\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$ (4)


Question 8
[12 marks]

Given: A: $f(x)=4^{x}$
a) Sketch $A$ and $A^{-1}$ on the same set of axes. Label all relevant points.

b) Determine $a$ if $f(a)=8$.
$\qquad$
$\qquad$
$\qquad$
c) Explain how you can use coordinates and transformation rules to determine $b$ if $f^{-1}(8)=b$ ?
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$\qquad$

