

# XT - MATHS Grade 12

Name: \_\_\_\_\_

Class: \_\_\_\_\_

Subject: Calculus 1: Factor Theorem

Date: \_\_\_\_\_

Total Marks: 76

Question 1: True/False [8]

Mathematics - LO 2 : AS 4

$$f(x) = 2x^3 - 9x^2 + 16x - 12$$

The only real root of  $f(x)$  is  $x = 2$ .

TRUE

FALSE

Question 2: True/False [8]

Mathematics - LO 2 : AS 4

$$f(x) = x^3 - 8x^2 + 5x + 14$$

If  $f(x) = 0$ , then  $x$  will be equal to 2 or 7.

TRUE

FALSE

Question 3: Multiple Choice [2]

Mathematics - LO 2 : AS 4

$f(x) = x^2 - x$  divided by  $x + 1$  leaves a remainder of ...

A 2

B -2

C 0

D 6

Question 4: Multiple Choice [4]

$$f(x) = x^3 + 2x^2 - 3x - 3$$

The number  $p$  which must be added to  $f(x)$  so that  $f(x) + p$  is exactly divisible by  $(2x - 1)$  is ...

A  $3\frac{7}{8}$

B  $-3\frac{7}{8}$

C  $3\frac{3}{8}$

D  $-3\frac{3}{8}$

E  $4\frac{1}{8}$

**Question 5: Multiple Choice [6]**

Mathematics - LO 2 : AS 4

If  $x - 2$  is a factor of  $f(x) = x^3 - 12x^2 + 44x - 48$ ,  
what is the solution of  $f(x) = 0$ ?

**A**  $x = 2; x = 4; x = 6$

**B**  $x = 2; x = 3; x = 4$

**C**  $x = -2; x = -4; x = -6$

**D**  $x = -2; x = -4; x = 18$

**Question 6: True/False [2]**

Mathematics - LO 2 : AS 4

If  $f(x)$  is a polynomial of the 3<sup>rd</sup> degree and

$f(x) = (2x + 3) \cdot Q(x) + 7$ , then  $f(x) - 7$  will be divisible by  $(2x + 3)$ .

 **TRUE** **FALSE****Question 7: True/False [3]**

Mathematics - LO 2 : AS 4

$(x + 2)$  is a factor of  $x^3 + 8x^2 + 17x + 10$ .

 **TRUE** **FALSE****Question 8: Socrates [8]**

Mathematics - LO 2 : AS 4

If  $f(x) = x^3 + ax^2 - 7x + b$  and  $g(x) = x^2 + x - 2$ , then  $a = \dots$  and  $b = \dots$   
Type in the two answers in order, separated by a ;

**Question 9: Socrates [4]**

Mathematics - LO 2 : AS 4

$$f(x) = x^3 + (k - 4)x^2 + (k - 9)x - 4$$

If  $f(x)$  divided by  $(x - 2)$  gives a remainder of 12, then the value of  $k$  will be ...  
Type the number only.

**Question 10: Socrates [4]**

Mathematics - LO 2 : AS 4

$$f(x) = 12x^3 + mx^2 + 10x - 8$$

If  $2x + 1$  is a factor of  $f(x)$ , then  $m = \dots$   
Type the number only.

**Question 11: Socrates [3]**

Mathematics - LO 2 : AS 4

When  $f(x) = 2x^3 - 7x^2 - 3x + 20$  is divided by  $2x + 3$ , the remainder is ...  
Type the number only.

**Question 12: Cloze [4]**

Mathematics - LO 2 : AS 4

$$f(x) = x^3 - 2x^2 - 2x + 7$$

If  $f(x)$  is divided by  $(x - a)$  and it leaves no remainder, then (Ans. 1).

If  $f(x)$  is divided by  $(x - 2)$  and the remainder is 3, then (Ans. 2).

When  $f(x)$  is divided by  $(2x - 1)$ , then the remainder is equal to (Ans. 3).

<b>1</b>	
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<b>2</b>	
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<b>3</b>	
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▶  $f(2) = 3$

▶  $f(-3) = 2$

▶  $f(a) = 0$

▶  $f(-2) = 3$

▶  $f(-a) = 0$

▶  $5\frac{5}{8}$

▶  $6\frac{1}{6}$

▶  $-\frac{1}{2}$

**Question 13: Cloze [6]**

Mathematics - LO 2 : AS 4

$$f(y) = 8y^3 + 26y^2 - 23y + 4 \text{ and } f\left(\frac{1}{2}\right) = 0.$$

The three roots in ascending order are: (Ans. 1), (Ans. 2) and (Ans. 3).

<b>1</b>	
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<b>2</b>	
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<b>3</b>	
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▶  $y = \frac{1}{2}$

▶  $y = -4$

▶  $y = \frac{1}{4}$

▶  $f = \frac{1}{2}$

▶  $f = -4$

▶  $f = \frac{1}{4}$

**Question 14: Cloze [10]**

Mathematics - LO 2 : AS 4

$$f(x) = x^3 + m^2x^2 - 25x - 14m$$

The value(s) of  $m$  for which  $x + 1$  will be a factor of  $f(x)$  is/are (Ans. 1).

The value(s) of  $m$  for which  $x - 4$  will be a factor of  $f(x)$  is/are (Ans. 2).

The value(s) of  $m$  for which the product of  $x + 1$  and  $x - 4$  will be a factor of  $f(x)$  is/are (Ans. 3).

<b>1</b>	
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<b>2</b>	
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<b>3</b>	
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▶  $m = 2; m = 12$

▶  $m = 2; m = -\frac{9}{8}$

▶  $m = 2; m = 12; m = -\frac{9}{8}$

▶  $m = 2$

▶  $m = -2; m = \frac{9}{8}$

▶  $m = -2; m = -12$

**Question 15: Socrates [4]**

Mathematics - LO 2 : AS 4

Is  $2x - 1$  a factor of  $f(x) = 4x^3 + 2x^2 + 2x - 2$ ?

Type either Yes or No.

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